

## Numbers in different bases

Binary base (radix). The only digits used are 0 and 1.

512	256	128	64	32	16	8	4	2	1
$2^9$	$2^8$	$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$

Consider the decimal number 139.

What is the highest power of 2 that will make 2 raised to that power just less than 139. This highest power is 7 and  $2^7 = 128$ .

Place a 1 under  $2^7$ .

$2^9$	$2^8$	$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$
		1							

Subtract  $139-128=11$ .

What is the highest power of 2 that will make 2 raised to that power just less than 11. The highest power is 3 and  $2^3 = 8$

Place a 1 under  $2^3$ .

$2^9$	$2^8$	$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$
						1			

Subtract  $11-8=3$ .

What is the highest power of 2 that will make 2 raised to that power just less than 3. The highest power is 1 and  $2^1 = 2$

Place a 1 under  $2^1$ .

$2^9$	$2^8$	$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$
						1		1	

Subtract  $3-2=1$ .

What is the highest power of 2 that will make 2 raised to that power just less than 1. The highest power is 0 and  $2^0 = 1$ .

Place a 1 under  $2^0$  so that finally

$2^9$	$2^8$	$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$
		1	0	0	0	1	0	1	1

Subtract  $2-1=1$ .

Thus expressed in binary, the number 139 is 10001011.

Note that,  $2+1 = 3$ , and in binary is  $10+01=11$ . Also  $2+2 = 4$  and in binary is  $10+10=100$ .

Ternary base (radix). The only digits used are 0, 1 and 2.

19683	6561	2187	729	243	81	27	9	3	1
$3^9$	$3^8$	$3^7$	$3^6$	$3^5$	$3^4$	$3^3$	$3^2$	$3^1$	$3^0$

Performing similar operations for decimal 139 for the ternary base system we have

$139 = 81 + 58 = 81 + 2.27 + 4 = 81 + 2.27 + 3 + 1$  so the ternary representation is

19683	6561	2187	729	243	81	27	9	3	1
$3^9$	$3^8$	$3^7$	$3^6$	$3^5$	$3^4$	$3^3$	$3^2$	$3^1$	$3^0$
					1	2	0	1	1

What is 139 decimal in the quaternary base system?

Show video "Alternative Math" (AM).

What is  $2 + 2$  (by "Alternative Math")?

In the binary system  $2 \rightarrow 10$ , so  $2 + 2 = 10 + 10 = 100$  (binary) = 4 (decimal) by ordinary binary addition.

But by "Alternative Math"  $10 + 10 = 1010$ .

Back in decimal, 1010 translates to  $1.8+0+1.2+0=10$  so by binary AM  $2 + 2 = 10$  decimal.

In the ternary system  $2 \rightarrow 2$ , so  $2 + 2 = 2 + 2 = 11$  (ternary) by ordinary ternary addition.

But by "Alternative Math"  $2 + 2 = 22$ .

Back in decimal this translates to  $2.3+2.1 = 8$  so by binary AM  $2 + 2 = 8$  decimal.

What is  $2+2$  in the quaternary base system?

In the quaternary base system, but using AM for  $2+2$  what is its result in the ordinary base 10 system?